

6 2 SOLVING MULTI STEP LINEAR INEQUALITIES

6 2 SOLVING MULTI STEP LINEAR INEQUALITIES IS AN ESSENTIAL SKILL IN ALGEBRA THAT ALLOWS STUDENTS TO UNDERSTAND AND SOLVE INEQUALITIES INVOLVING MULTIPLE STEPS. LINEAR INEQUALITIES ARE SIMILAR TO LINEAR EQUATIONS BUT INCLUDE AN INEQUALITY SYMBOL ($<$, $>$, $\leq$, $\geq$) RATHER THAN AN EQUAL SIGN. THIS ARTICLE WILL EXPLORE THE CONCEPT OF MULTI-STEP LINEAR INEQUALITIES, THE TECHNIQUES USED TO SOLVE THEM, AND PROVIDE EXAMPLES TO ILLUSTRATE THESE TECHNIQUES.

UNDERSTANDING LINEAR INEQUALITIES

LINEAR INEQUALITIES CAN BE EXPRESSED IN THE FORM:

- $AX + B < C$
- $AX + B > C$
- $AX + B \leq C$
- $AX + B \geq C$

WHERE:

- A, B, AND C ARE CONSTANTS.
- X REPRESENTS THE VARIABLE WE WANT TO SOLVE FOR.

THE MAIN DIFFERENCE BETWEEN LINEAR EQUATIONS AND LINEAR INEQUALITIES IS THAT INEQUALITIES DO NOT HAVE A SINGLE SOLUTION BUT RATHER A RANGE OF SOLUTIONS. FOR EXAMPLE, THE INEQUALITY $x + 3 < 7$ MEANS THAT X CAN BE ANY NUMBER LESS THAN 4.

CHARACTERISTICS OF LINEAR INEQUALITIES

BEFORE DIVING INTO THE SOLVING PROCESS, IT'S CRUCIAL TO UNDERSTAND A FEW IMPORTANT CHARACTERISTICS OF LINEAR INEQUALITIES:

1. INEQUALITY SYMBOLS: THE SYMBOLS USED IN INEQUALITIES CONVEY DIFFERENT MEANINGS:

- ' $<$ ' MEANS "LESS THAN."
- ' $>$ ' MEANS "GREATER THAN."
- ' $\leq$ ' MEANS "LESS THAN OR EQUAL TO."
- ' $\geq$ ' MEANS "GREATER THAN OR EQUAL TO."

2. GRAPHICAL REPRESENTATION: THE SOLUTION TO A LINEAR INEQUALITY CAN BE REPRESENTED ON A NUMBER LINE OR CARTESIAN PLANE. A SOLID DOT IS USED TO INDICATE THAT A NUMBER IS INCLUDED IN THE SOLUTION ($\leq$ OR $\geq$), WHILE AN OPEN DOT INDICATES THAT IT IS NOT INCLUDED ($<$ OR $>$).

3. DIRECTION OF INEQUALITY: WHEN MULTIPLYING OR DIVIDING BOTH SIDES OF AN INEQUALITY BY A NEGATIVE NUMBER, THE DIRECTION OF THE INEQUALITY SYMBOL MUST BE REVERSED. FOR EXAMPLE, IF $-2x > 6$, DIVIDING BY -2 WOULD CHANGE IT TO $x < -3$.

STEPS FOR SOLVING MULTI-STEP LINEAR INEQUALITIES

SOLVING MULTI-STEP LINEAR INEQUALITIES INVOLVES SEVERAL STEPS. HERE'S A SYSTEMATIC APPROACH:

STEP 1: SIMPLIFY EACH SIDE

BEGIN BY SIMPLIFYING BOTH SIDES OF THE INEQUALITY. THIS MAY INVOLVE:

- COMBINING LIKE TERMS.
- DISTRIBUTING ANY COEFFICIENTS.

FOR EXAMPLE, IN THE INEQUALITY $3(x + 2) > 9$, DISTRIBUTE THE 3:

$$3x + 6 > 9.$$

STEP 2: ISOLATE THE VARIABLE

NEXT, ISOLATE THE VARIABLE ON ONE SIDE OF THE INEQUALITY. THIS CAN BE DONE BY PERFORMING INVERSE OPERATIONS, SIMILAR TO SOLVING EQUATIONS. KEEP THE INEQUALITY SYMBOL INTACT THROUGHOUT THE PROCESS.

USING THE PREVIOUS EXAMPLE, SUBTRACT 6 FROM BOTH SIDES:

$$3x > 3.$$

THEN, DIVIDE BY 3:

$$x > 1.$$

STEP 3: GRAPH THE SOLUTION

ONCE YOU HAVE ISOLATED THE VARIABLE, GRAPH THE SOLUTION ON A NUMBER LINE TO VISUALIZE THE SET OF POSSIBLE VALUES FOR x . FOR $x > 1$, YOU WOULD DRAW AN OPEN DOT AT 1 AND SHADE TO THE RIGHT, INDICATING ALL VALUES GREATER THAN 1.

STEP 4: CHECK YOUR SOLUTION

TO ENSURE ACCURACY, SUBSTITUTE A NUMBER FROM THE SOLUTION SET BACK INTO THE ORIGINAL INEQUALITY. IF IT HOLDS TRUE, YOUR SOLUTION IS CORRECT.

FOR EXAMPLE, IF YOU TAKE $x = 2$ (WHICH IS GREATER THAN 1), SUBSTITUTE IT BACK INTO THE ORIGINAL INEQUALITY:

$$3(2 + 2) > 9.$$

THIS SIMPLIFIES TO $12 > 9$, WHICH IS TRUE, CONFIRMING THAT THE SOLUTION IS CORRECT.

EXAMPLES OF SOLVING MULTI-STEP LINEAR INEQUALITIES

LET'S LOOK AT A FEW EXAMPLES TO ILLUSTRATE THE PROCESS OF SOLVING MULTI-STEP LINEAR INEQUALITIES.

EXAMPLE 1: SOLVING A SIMPLE INEQUALITY

SOLVE THE INEQUALITY: $4x - 5 \leq 3$.

STEP 1: ADD 5 TO BOTH SIDES:

$$4x \leq 8.$$

STEP 2: DIVIDE BY 4:

$$x \leq 2.$$

STEP 3: GRAPH THE SOLUTION:

- DRAW A SOLID DOT AT 2 AND SHADE TO THE LEFT.

STEP 4: CHECK THE SOLUTION:

SUBSTITUTING $x = 2$:

$$4(2) - 5 \leq 3$$

$$8 - 5 \leq 3$$

$$3 \leq 3 \text{ (TRUE).}$$

EXAMPLE 2: SOLVING A MORE COMPLEX INEQUALITY

SOLVE THE INEQUALITY: $2(x - 3) + 4 > 3(x + 1)$.

STEP 1: DISTRIBUTE BOTH SIDES:

$$2x - 6 + 4 > 3x + 3.$$

STEP 2: SIMPLIFY:

$$2x - 2 > 3x + 3.$$

STEP 3: ISOLATE x BY MOVING TERMS:

$$-2 > 3x - 2x + 3,$$

$$-2 > x + 3.$$

SUBTRACT 3 FROM BOTH SIDES:

$$-5 > x.$$

THIS CAN ALSO BE EXPRESSED AS $x < -5$.

STEP 4: GRAPH THE SOLUTION:

- DRAW AN OPEN DOT AT -5 AND SHADE TO THE LEFT.

STEP 5: CHECK THE SOLUTION:

SUBSTITUTING $x = -6$:

$$2(-6 - 3) + 4 > 3(-6 + 1),$$

$$-18 + 4 > -15,$$

$$-14 > -15 \text{ (TRUE).}$$

EXAMPLE 3: AN INEQUALITY WITH VARIABLES ON BOTH SIDES

SOLVE THE INEQUALITY: $3x + 7 < 2x + 12$.

STEP 1: MOVE ALL TERMS INVOLVING x TO ONE SIDE:

$$3x - 2x < 12 - 7,$$
$$x < 5.$$

STEP 2: GRAPH THE SOLUTION:

- DRAW AN OPEN DOT AT 5 AND SHADE TO THE LEFT.

STEP 3: CHECK THE SOLUTION:

SUBSTITUTING $x = 4$:

$$3(4) + 7 < 2(4) + 12,$$
$$12 + 7 < 8 + 12,$$
$$19 < 20 \text{ (TRUE).}$$

COMMON MISTAKES TO AVOID

WHEN SOLVING MULTI-STEP LINEAR INEQUALITIES, STUDENTS OFTEN MAKE SEVERAL COMMON MISTAKES:

1. FORGETTING TO REVERSE THE INEQUALITY: REMEMBER TO REVERSE THE INEQUALITY SYMBOL WHEN MULTIPLYING OR DIVIDING BY A NEGATIVE NUMBER.
2. NEGLECTING TO GRAPH: ALWAYS GRAPH THE SOLUTION FOR BETTER COMPREHENSION, AS VISUALIZING THE SOLUTION SET CAN HELP IN UNDERSTANDING THE RESULTS.
3. SKIPPING THE CHECK: ALWAYS CHECK YOUR SOLUTION BY SUBSTITUTING IT BACK INTO THE ORIGINAL INEQUALITY TO VERIFY CORRECTNESS.

CONCLUSION

MASTERING THE SKILL OF SOLVING MULTI-STEP LINEAR INEQUALITIES IS VITAL FOR SUCCESS IN ALGEBRA AND ADVANCED MATHEMATICS. BY FOLLOWING A SYSTEMATIC APPROACH—SIMPLIFYING EACH SIDE, ISOLATING THE VARIABLE, GRAPHING THE SOLUTION, AND CHECKING THE RESULT—YOU CAN CONFIDENTLY TACKLE A WIDE RANGE OF INEQUALITIES. AS YOU PRACTICE, THESE TECHNIQUES WILL BECOME SECOND NATURE, ENABLING YOU TO SOLVE COMPLEX PROBLEMS WITH EASE.

FREQUENTLY ASKED QUESTIONS

WHAT ARE MULTI-STEP LINEAR INEQUALITIES AND HOW DO THEY DIFFER FROM LINEAR EQUATIONS?

MULTI-STEP LINEAR INEQUALITIES INVOLVE EXPRESSIONS THAT INCLUDE INEQUALITIES (LIKE $<$, $>$, $\leq$, OR $\geq$) AND REQUIRE MULTIPLE STEPS TO ISOLATE THE VARIABLE, SIMILAR TO SOLVING LINEAR EQUATIONS. THE MAIN DIFFERENCE IS THAT WHEN YOU MULTIPLY OR DIVIDE BY A NEGATIVE NUMBER, YOU MUST REVERSE THE INEQUALITY SIGN.

HOW DO YOU SOLVE THE INEQUALITY $2x - 3 < 7$ STEP BY STEP?

TO SOLVE $2x - 3 < 7$, FIRST ADD 3 TO BOTH SIDES TO GET $2x < 10$. THEN, DIVIDE BOTH SIDES BY 2 TO ISOLATE x , RESULTING IN $x < 5$. THE SOLUTION MEANS ANY NUMBER LESS THAN 5 SATISFIES THE INEQUALITY.

CAN YOU PROVIDE AN EXAMPLE OF A MULTI-STEP LINEAR INEQUALITY INVOLVING PARENTHESES?

SURE! CONSIDER THE INEQUALITY $3(2x + 4) > 12$. FIRST, DISTRIBUTE THE 3 TO GET $6x + 12 > 12$. NEXT, SUBTRACT 12 FROM BOTH SIDES TO YIELD $6x > 0$, AND FINALLY DIVIDE BY 6 TO FIND $x > 0$.

WHAT IS THE IMPORTANCE OF GRAPHING THE SOLUTION SET FOR LINEAR INEQUALITIES?

GRAPHING THE SOLUTION SET FOR LINEAR INEQUALITIES VISUALLY REPRESENTS THE RANGE OF SOLUTIONS AND HELPS IN UNDERSTANDING HOW THE INEQUALITY BEHAVES. IT ALSO ALLOWS FOR EASY IDENTIFICATION OF BOUNDARY POINTS, WHICH ARE CRUCIAL FOR DETERMINING WHETHER SOLUTIONS ARE INCLUDED OR EXCLUDED.

HOW DO YOU HANDLE INEQUALITIES THAT INVOLVE ABSOLUTE VALUES IN MULTI-STEP LINEAR INEQUALITIES?

WHEN DEALING WITH ABSOLUTE VALUE INEQUALITIES, SUCH AS $|x - 3| < 5$, YOU SPLIT IT INTO TWO SEPARATE INEQUALITIES: $x - 3 < 5$ AND $x - 3 > -5$. SOLVE EACH INEQUALITY TO FIND THE RANGE OF SOLUTIONS, WHICH IN THIS CASE RESULTS IN THE COMBINED SOLUTION $-2 < x < 8$.

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